

**EVALUATING  
ACADEMIC READINESS  
FOR APPRENTICESHIP TRAINING**  
Revised for  
**ACCESS TO APPRENTICESHIP**

**MATHEMATICS SKILLS  
OPERATIONS WITH FRACTIONS**

**AN ACADEMIC SKILLS MANUAL  
for**

**The Food Preparation Trades**

This trade group includes the following trades:  
Baker & Cook and Retail Meat Cutter

*Workplace Support Services Branch  
Ontario Ministry of Education and Training*

*Revised 2011*

In preparing these Academic Skills Manuals we have used passages, diagrams and questions similar to those an apprentice might find in a text, guide or trade manual.

**This trade related material is not intended to instruct you in your trade. It is used only to demonstrate how understanding an academic skill will help you find and use the information you need.**

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# MATHEMATICS SKILLS

## OPERATIONS WITH FRACTIONS

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*An academic skill required for the study of the  
Food Preparation Trades*

### **INTRODUCTION**

During a day at work, you will come across situations like these.

You are asked to double a bread recipe that calls for  $7\frac{1}{2}$  pounds of flour.

You are going to cut 60 rib eye steaks. Each is to weight  $5\frac{1}{2}$  ounces. How much rib eye will you need?

When you slice pie, you cut each pie into eight pieces. If you have one half of an apple pie, three quarters of a lemon pie and  $2\frac{6}{8}$  of a lemon pie. How many slices of pie can you serve?

To carry out these kinds of tasks, you need to use numbers to get information and, likely, to give the information to someone else. Some numbers, such as  $\frac{5}{16}$ ,  $\frac{1}{2}$ ,  $\frac{1}{32}$  and  $\frac{3}{4}$ , are fractions. An understanding of how to add, subtract, multiply and divide fractions will be useful in many situations.

This skills manual covers the following information about fractions:

- ◆ What is a fraction?
- ◆ Equivalent fractions and lowest terms
- ◆ Adding fractions
  - fractions with the same denominator
  - fractions with different denominators
  - adding more than two fractions
  - adding mixed numbers
- ◆ Subtracting fractions
- ◆ Multiplying fractions
- ◆ Dividing fractions
- ◆ Using a calculator

### **WHAT IS A FRACTION?**

Terms such as one half and three quarters indicate partial amounts of an original whole. They are called fractions. A **fraction** is a mathematical shorthand used to indicate a part of a whole.

Let's examine what fractions are by looking at the inch divisions on a ruler. See Figure 1.

Each 1 inch division can be divided into smaller, equal spaces. If an inch is divided into two equal spaces, the spaces are **one half** of an inch. Two one half spaces equal one inch.

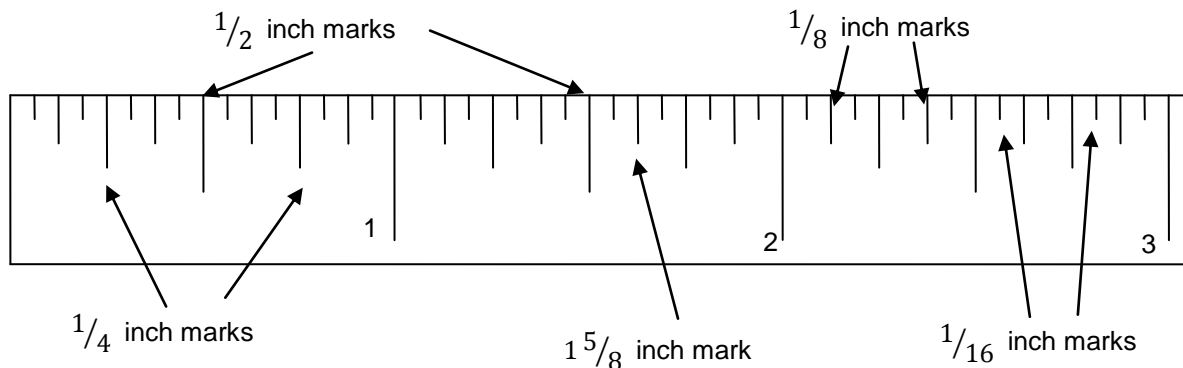


Figure 1: Imperial Ruler

If a one inch division is divided into four equal spaces, each space is **one fourth**, or **one quarter** of an inch. So 4 one quarter inch spaces equal one inch. A measurement that is three of the quarter inch divisions is called three quarters of an inch.

### Writing Fractions

Fractions can be written in several ways. Here are different ways to write the fraction three quarters.

- three quarters
- $\frac{3}{4}$
- 3 out of 4
- three fourths
- $\frac{3}{4}$

A **fraction** is written to indicate a part of a whole.

1. Numerically, a fraction is written with two numerals separated by a fraction line.
2. *The digit under the fraction line is the **denominator**. It tells how many parts the whole thing was divided into.*
  - In the fraction  $\frac{3}{4}$  the denominator, 4, tells how many parts the whole thing is divided into.
3. *The digit above the fraction line is the **numerator**. It tells how many of the total parts we have.*
  - In the fraction  $\frac{3}{4}$  the numerator, 3, tells how many of the total parts we have.
4. We have  $\frac{3}{4}$  of something, or three parts of the total of four.

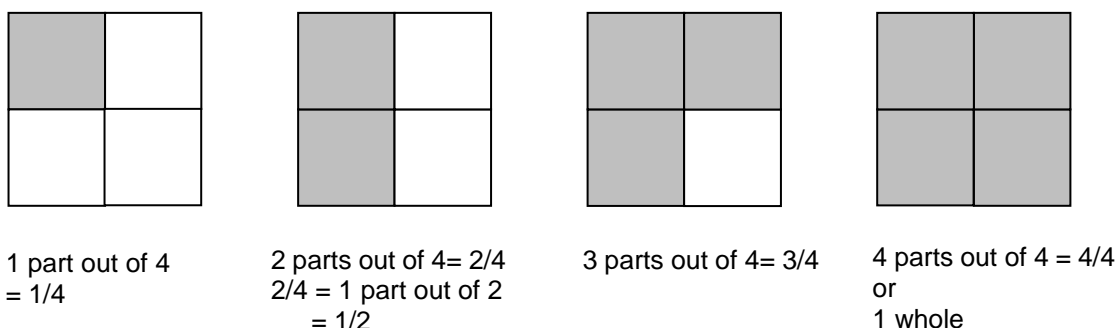
Remember that the **d**enominator is **d**own under the fraction line.

## Fractions are part of something whole

A fraction represents *part* of an original whole that has been divided into equal pieces.

Look at Figure 2 as you read the following. Consider a pound of butter that is divided into 4 equal pieces. If you use 2 out of the 4 pieces, you use  $\frac{2}{4}$  of the total. You can see that this is the same amount as  $\frac{1}{2}$  of the sheet. Two pieces out of four is the same as one out of two. You can write  $\frac{2}{4}$  as  $\frac{1}{2}$ .

Four pieces out of four are equal to all of the original amount or one whole.  $\frac{4}{4}$  equals all of the sheet or 1. Even though the butter is now cut into 4 pieces, you still have the same total amount.



**FIGURE 2: A Fraction Is A Part Of A Whole**

**Naming fractions:**  $\frac{1}{2}$  is written in words as one half.  $\frac{1}{3}$  is written as one third.  $\frac{1}{4}$  is written as one quarter or one fourth. The other fractions are written by adding *th* to the name of the denominator. If we divide a pound of butter into four pieces, we say it is divided into fourths. If it is divided into twenty equal pieces, we say the butter is divided into twentieths. If we have eleven out of the twenty pieces, we have eleven twentieths.

### *Fractions Mean Something is Divided*

Division is a way of splitting a number into *equal, smaller* numbers. For example, a group of 12 eggs can be divided into 3 smaller groups of 4 eggs each.  $12 \div 3 = 4$  (Sometimes when we divide a number we have a leftover amount known as a remainder.  $13 \div 3 = 4 \text{ R}1$ )

Fractions are a way of indicating a division question in which the numerator is divided by the denominator.

$\frac{3}{4}$  is the same as  $3 \div 4$   
 $\frac{1}{2}$  is the same as  $1 \div 2$   
 $\frac{12}{3}$  is the same as  $12 \div 3$   
 $\frac{8}{5}$  is the same as  $8 \div 5$

When you use a number as a fraction, you don't actually do the division. If you do the division, the answer will be one of these: a whole number, a whole number with a remainder or a decimal number.

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### **Mixed Numbers and Improper Fractions**

You can have one or more whole objects along with part of an object.

**Example:** You might have three whole litres and one half litre of olive oil. This is written  $3\frac{1}{2}$  litres, and read as three and a half litres.

A number like  $3\frac{1}{2}$ , consisting of a whole number and a fraction, is called a mixed number.

*A mixed number is a combination of a whole number and a fraction.*

- A mixed number such as  $3\frac{1}{2}$  can be written as the fraction  $\frac{7}{2}$ , *with the whole number included in the numerator.*
  - The 3 whole numbers are each divided into 2 halves, just like the inch division on a ruler.
  - This gives a total of 6 halves.
  - If you add the 6 halves to the 1 half, you have 7 halves.
  - Seven halves can be written  $\frac{7}{2}$ .

*An improper fraction is a fraction with the numerator larger than the denominator.*

- The form  $\frac{7}{2}$ , in which the numerator is larger than the denominator, is an improper fraction.

You can change a mixed number like  $3\frac{1}{2}$  to an improper fraction like  $\frac{7}{2}$ . You can also change an improper fraction into a mixed number.

- ◆ In fact, in order to multiply or divide with numbers that include fractions, you must ***change all mixed numbers to improper fractions before multiplying or dividing.***
- ◆ On the other hand, when you get an improper fraction as the answer to a question, ***the improper fraction is usually changed to a mixed number.***

So you need to know how to change a mixed number such as  $1\frac{1}{4}$  to the improper fraction  $\frac{5}{4}$ . You also need to know how to change an improper fraction such as  $\frac{11}{4}$  to the mixed number  $2\frac{3}{4}$ .

#### **To change a mixed number to an improper fraction:**

1. Multiply the *whole number* by the *denominator* of the fraction.
2. Add this *answer* to the *original numerator* to get the *new numerator*.
3. Write the *new numerator* over the fraction line and the *original denominator* under it. Notice the denominator stays the same.

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**Example:** Change  $3 \frac{2}{5}$  to an improper fraction.

$3 \times 5 = 15$                   Multiply the whole number 3 by the denominator 5..

$15 + 2 = 17$                 Add 15 to the numerator to get the new numerator of the improper fraction.

Replace the original numerator with the new numerator.  
Put 17 over the original denominator 5 to get the improper fraction  $17/5$ .

The mixed number  $3 \frac{2}{5}$  is the improper fraction  $17/5$ .

**To change an improper fraction to a mixed number:**

1. Divide the numerator by the denominator until you have a remainder.
2. Your *answer* becomes the *whole number*.
3. The *remainder* forms the *numerator* of the fractional part.
4. It is written over the fraction line above the *original denominator*.

**Example:** Change  $14/3$  to a mixed number.

$14 \div 3 = 4$  with remainder 2                  4 becomes the whole number.  
remainder 2 becomes the numerator.  
the denominator 3 remains the same

The improper fraction  $14/3$  is the mixed number  $4 \frac{2}{3}$ .

**Note:** If the fraction is not already in lowest terms, it should be reduced to lowest terms. We will look at how to do this later.

**There are a few unusual cases that you should recognize.**

1. An improper fraction will end up as a whole number if the denominator divides evenly into the numerator.

**Example:**  $9/3 = 3$

2. Any fraction with the same numerator and denominator is equal to one.

**Example:**  $4/4 = 1$

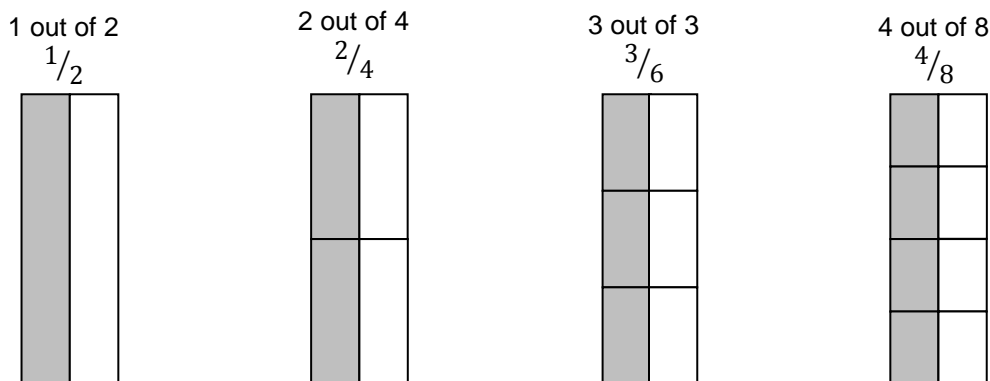
**Note:** Multiplying or dividing any number by 1 does not change the value of the number. So multiplying or dividing a number by 1 expressed as a fraction such as  $4/4$  does not change the value of the number.

3. Any whole number may be written as a fraction by putting it over 1. This step will be used later when dividing a fraction by a whole number.

**Example:**  $8 = 8/1$

## EQUIVALENT FRACTIONS AND LOWEST TERMS

When you cut a loaf of French bread down the middle, dividing it evenly into two pieces, each piece is half ( $1/2$ ) of the whole loaf. Look at the diagram.



**FIGURE 3: Equivalent Fractions**

$1/2, 2/4, 3/6, 4/8$  are equivalent fractions.

The shaded areas all represent the same amount.

You see that if you cut the loaf into 4 equal pieces and use two fourths ( $2/4$ ), you would, again, use  $1/2$  of the loaf. If you cut the bread into six equal parts, you see that 3 of those 6 pieces, or  $3/6$  of the whole loaf, is the same as  $1/2$  of the sheet. If you cut the loaf into 8 equal pieces, you see that 4 of the 8 pieces,  $4/8$ , is also equal to  $1/2$ .

The fractions  $2/4, 3/6$  and  $4/8$  each represent the same amount as  $1/2$ . They are equivalent fractions; that is, they are the same as or equal to  $1/2$ . They represent the same partial amount of the whole. Because  $4/8, 3/6, 2/4$  and  $1/2$  represent the same amount, they are called **equivalent fractions**.

### Making an Equivalent Fraction

Let's take a closer look at equivalent fractions, starting with  $1/2$  and  $2/4$ .

- ◆ Notice that by multiplying both the numerator and the denominator of  $1/2$  by 2, we get  $2/4$ .

$$\begin{array}{l} \underline{1} \times 2 = \underline{2} \\ \underline{2} \times 2 = \underline{4} \end{array}$$

- ◆ And, if we divide both the numerator and the denominator of  $2/4$  by 2, we get  $1/2$ .

$$\begin{array}{l} \underline{2} \div 2 = \underline{1} \\ \underline{4} \div 2 = \underline{2} \end{array}$$

Look next at the equivalent fractions  $\frac{1}{2}$  and  $\frac{3}{6}$ .

- ◆ If we multiply both the numerator and the denominator of  $\frac{1}{2}$  by 3, we get  $\frac{3}{6}$ .

$$\frac{1}{2} \times 3 = \frac{3}{6}$$

- ◆ And if we divide both the numerator and the denominator of  $\frac{3}{6}$  by 3, we get  $\frac{1}{2}$ .

$$\frac{3}{6} \div 3 = \frac{1}{2}$$

Now look at  $\frac{1}{2} = \frac{4}{8}$

$$\frac{1 \times 4}{2 \times 4} = \frac{4}{8}$$

And

$$\frac{4 \div 4}{8 \div 4} = \frac{1}{2}$$

In each case, we changed one fraction into an equivalent fraction by multiplying or dividing.

**To make an equivalent fraction with a larger denominator:**

1. Multiply both the denominator and the numerator of the fraction by the same number.
2. Use the answers from the multiplication to form the numerator and denominator of the equivalent fraction.

**Example:** Using the fraction  $\frac{2}{5}$ , make an equivalent fraction by multiplying by  $\frac{3}{3}$ .

$$\frac{2}{5} \times \frac{3}{3}$$

Multiply both the numerator and denominator by 3.

In other words, multiply the fraction by  $\frac{3}{3}$ .

$$= \frac{6}{15}$$

The equivalent fraction is  $\frac{6}{15}$ .

**Example:** Change  $\frac{2}{3}$  to an equivalent fraction by multiplying by  $\frac{4}{4}$ .

$$\frac{2}{3} = \frac{8}{12}$$

Multiply both the numerator 2 and the denominator 3 by 4.

**Example:** Change  $\frac{3}{4}$  to an equivalent fraction by multiplying by  $\frac{5}{5}$ .

$$\frac{3}{4} = \frac{15}{20}$$

You also will be given a fraction and only the denominator of a new, equivalent fraction. You have to find the numerator of the second fraction.

**Example:** You might need to change the fraction  $\frac{2}{3}$  to an equivalent fraction with a denominator of 12. Write the second fraction as  $\frac{?}{12}$  until you find the numerator.

**To find an equivalent fraction when one fraction and the denominator of an equivalent fraction are known:**

1. Divide the larger denominator by the smaller denominator.
2. Multiply the numerator and denominator of the original fraction by the division answer.
3. The resulting answer is the equivalent fraction.

**Example:** Find an equivalent fraction to  $\frac{2}{3}$  whose denominator is 12.

In other words,  $\frac{2}{3} = \frac{?}{12}$ .

$$12 \div 3 = 4 \quad \text{Divide 12 by 3.}$$

$$\frac{2}{3} \times \frac{4}{4} \quad \text{Multiply the numerator 2 and the denominator 3 by the division answer 4.}$$

The fraction that is equivalent to  $\frac{2}{3}$  and that has a denominator of 12 is  $\frac{8}{12}$ .

**Example:**  $\frac{3}{4} = \frac{?}{20}$

$$20 \div 4 = 5 \quad \text{Divide 20 by 4.}$$

$$\frac{3}{4} \times \frac{5}{5} \quad \text{Multiply the numerator 3 and the denominator 4 by the division answer 5.}$$

$$\frac{3}{4} = \frac{15}{20}$$

**Example:**  $\frac{1}{6} = \frac{?}{18}$

$$18 \div 6 = 3 \quad \text{Divide 18 by 6.}$$

$$\frac{1}{6} \times \frac{3}{3} \quad \text{Multiply the numerator 1 and the denominator 6 by the division answer 3.}$$

$$\frac{1}{6} = \frac{3}{18}$$

### ***Fractions in Their Lowest Terms***

When you finish a question, change any improper fractions to mixed numbers. Next, write the fraction answer as the ***smallest equivalent fraction***. This is called ***reducing to lowest terms***.

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Any number that will divide evenly into both the numerator and denominator is a **common factor**:

- 5 divides into both 10 and 15, so it is a common factor of 10 and 15.

A common factor could be one of the numbers *in the fraction*:

- 6 divides into 6 and 18, so 6 is a common factor.

**To reduce a fraction to lowest terms:**

1. Look for a common factor:
  - if there is none, the fraction is already in its lowest terms.
2. If you see a common factor, divide both the numerator and denominator by that number.
3. Write the division answers as the new numerator and denominator.
4. Look for another common factor:
  - if there is one, repeat the steps.
5. If there are no more common factors, the fraction is in its lowest terms.

If you aren't sure if there are any common factors, try **two, three or five**. If one of them divides evenly into both the numerator and the denominator, start with that.

**Example:** Reduce  $16/24$  to lowest terms.

$$\frac{16 \div 2}{24 \div 2} \quad 2 \text{ is a common factor; divide the numerator and denominator by } 2$$

$$= 8/12 \quad \text{Try to do it again.}$$

$$\frac{8 \div 4}{12 \div 4} \quad \text{It is now easy to see that } 4 \text{ will divide evenly into } 8 \text{ and } 12$$

$$= 2/3 \quad \text{The fraction is in its lowest terms.}$$

You might have seen immediately that 8 is a common factor and divided by it, getting the lowest term fraction  $2/3$  in one step. The larger the common factor you use, the fewer steps you need to use, but the final answer will be the same.

**Example:** Reduce  $15/35$  to lowest terms.

$$\frac{15 \div 5}{35 \div 5} \quad 5 \text{ is the common factor}$$

$$= 3/7$$

**Example:** Reduce  $18/24$  to lowest terms.

$$\frac{18 \div 6}{24 \div 6} \text{ 6 is the common factor}$$
$$= 3/4$$

### TO CHANGE A MIXED NUMBER TO AN IMPROPER FRACTION

1. Multiply the whole number by the denominator.
2. Add the answer to the numerator.
3. Place this new numerator over the original denominator.

1. Change the following mixed numbers to improper fractions. **Answers are at the end of this skills manual.**

a)  $3 \frac{2}{7} =$

b)  $1 \frac{5}{6} =$

c)  $5 \frac{1}{4} =$

d)  $2 \frac{7}{8} =$

e)  $10 \frac{2}{3} =$

f)  $6 \frac{1}{5} =$

### TO REDUCE FRACTIONS TO THEIR LOWEST TERMS

1. Find a common factor.
2. Divide both the numerator and the denominator by the common factor.
3. Write the division answers as the new numerator and denominator.
4. Check to see if there is a common factor for this fraction. If so, repeat steps 1 and 2 until there is no longer a common factor.

2. Reduce these fractions to their lowest terms.

a)  $6/9$

b)  $8/24$

c)  $15/60$

d)  $54/27$

e)  $9/72$

f)  $32/80$

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**TO CHANGE AN IMPROPER FRACTION TO A MIXED NUMBER**

1. Divide the numerator by the denominator. Your answer becomes the whole number.
2. The remainder forms the new numerator. Write it over the original denominator.
3. Reduce the fraction to its lowest terms.

3. Change the following improper fractions to mixed numbers and reduce to lowest terms.  
**Answers are at the end of this skills manual.**

a)  $12/9 =$

b)  $15/5 =$

c)  $23/7 =$

d)  $99/10 =$

e)  $6/1 =$

f)  $10/4 =$

4. Find the equivalent fraction.

a)  $3/5 = ?/40$

b)  $1/3 = ?/9$

c)  $10/3 = ?/18$

d)  $5/8 = ?/24$

e)  $1/4 = ?/12$

f)  $2/7 = ?/21$

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## **ADDING FRACTIONS**

In order to add fractions, all of the fractions must have a common (the same) denominator. To add fractions that do not have a common denominator, we have to make all of the fractions into equivalent fractions with the same denominators.

First let's look at adding fractions which already have common denominators.

### ***Adding Fractions with Common Denominators***

1. Add all the numerators together.
2. Write the sum over the original denominator.
3. Change any improper fraction to a mixed number.
4. Reduce the answer to lowest terms.

**Example:** Add  $5/9 + 7/9$

$$\begin{aligned}5 + 7 &= 12 \\5/9 + 7/9 &= 12/9 \\12/9 &= 1 \frac{3}{9} \\1 \frac{3}{9} &= 1 \frac{1}{3}\end{aligned}$$

1. Add the numerators together.
2. Place the new numerator 12 over the original denominator 9.
3. Change the improper fraction to a mixed number:
4. Divide by the common factor 3 to reduce to lowest terms.

**Example:**  $3/8 + 1/8 =$

$$\begin{aligned}\frac{3}{8} + \frac{1}{8} &= \frac{4}{8} \\&= 1/2\end{aligned}$$

- add the numerators  
put the answer over the denominator 8  
  
reduce to lowest terms

**Example:** Add  $5/16 + 3/16 + 1/16 =$

$$\frac{5}{16} + \frac{3}{16} + \frac{1}{16} = \frac{9}{16}$$

**Example:** Add  $5/12 + 11/12 + 1/12$

$$\begin{aligned}\frac{5}{12} + \frac{11}{12} + \frac{1}{12} &= \frac{17}{12} && \text{improper fraction} \\&= 1 \frac{5}{12} && \text{change to a mixed number}\end{aligned}$$

### ***Adding Mixed Numbers***

Adding mixed numbers follows the same steps as adding fractions, with the additional step of adding the whole numbers.

**To add mixed numbers:**

1. First add the whole numbers.
2. Then add the fractions.
3. Combine both answers.
4. If the fraction part of the answer is an improper fraction, change it to a mixed number.
5. Add the two whole numbers. Combine the answer with the new fraction.

**Example:**  $3 \frac{2}{5} + 1 \frac{1}{5}$

$$\begin{array}{r} \cdot \\ 3 + 1 = 4 \end{array} \quad 1. \text{ Add the whole numbers}$$

$$2/5 + 1/5 = 3/5 \quad 2. \text{ Add the fractions.}$$

$$4 + 3/5 = 4 \frac{3}{5} \quad 3. \text{ Combine the answers.}$$

**Example:**  $1 \frac{5}{8} + 2 \frac{7}{8}$

$$1 + 2 = 3 \quad 1. \text{ Add the whole numbers}$$

$$\begin{array}{r} 5/8 + 7/8 = 12/8 \\ 12/8 = 1 \frac{4}{8} \end{array} \quad \begin{array}{l} 2. \text{ Add the fractions.} \\ 3. \text{ Change the improper fraction to a mixed number and} \end{array}$$

$$1 \frac{4}{8} = 1 \frac{1}{2} \quad 4. \text{ Reduce the fraction to its lowest terms.}$$

$$3 + 1 \frac{1}{2} = 4 \frac{1}{2} \quad 5. \text{ Combine the whole numbers and write the answer as a mixed number with its fraction.}$$

**TO ADD FRACTIONS OR MIXED NUMBERS WITH THE SAME DENOMINATOR**

1. Add all the whole numbers if there are any.
2. Add all the numerators together.
3. Write the sum of the numerators over the original denominator.
4. If the sum is an improper fraction, change to a mixed number and add any whole numbers together.
5. Reduce the fraction to lowest terms.

Add these fractions. **Answers are at the end of this skills manual.**

5. a)  $2/7 + 4/7$

b)  $3/4 + 1/4$

c)  $5/8 + 7/8$

d)  $6 \frac{2}{5} + 1/5$

e)  $9 \frac{2}{3} + 4 \frac{2}{3}$

f)  $4 \frac{1}{6} + 8 \frac{5}{6}$

g)  $1/8 + 5/8 + 3/8$

h)  $4 \frac{1}{12} + 5/12 + 3 \frac{5}{12}$

i)  $5 \frac{1}{10} + 2 \frac{3}{10} + 7/10$

6. If you poured  $1 \frac{1}{3}$  liters of milk into a container that already contained  $3 \frac{1}{3}$  liters, how much milk would now be in the container?

### ***Adding Fractions That Have Different Denominators***

Remember, we can add fractions only if they have the same denominators. *If fractions have denominators that are different, we cannot add them until they are all changed into **equivalent fractions** that have the same denominator, called a **common denominator**.* A common denominator is one which can be evenly divided by any of the denominators in the addition question.

**To change denominators to a common denominator follow these steps:**

1. Figure out what the common denominator is going to be.
2. Change the fractions to equivalent fractions with that common denominator.
3. Add the equivalent fractions by adding the numerators and putting the answer over the common denominator.
4. Change any improper fraction to a mixed number. Reduce to lowest terms if necessary.

### **Step 1: Find a common denominator**

Finding a common denominator is mostly a case of trying out different methods until you get a number that will work.

***Method 1:*** *If one denominator will divide evenly into the other, use the larger number as the common denominator.*

**Example:** Find a common denominator of  $\frac{3}{4}$  and  $\frac{5}{8}$ . The denominators are 4 and 8.  
4 will divide evenly into 8.  
We can use 8 as a common denominator.

***Method 2:*** *A **common factor** is a number that will divide evenly into two or more other numbers.*

#### **Examples:**

2 is a common factor of 6 and 8.

3 is a common factor of 9 and 15.

If fractions such as  $\frac{3}{10}$  and  $\frac{4}{15}$  have denominators with a common factor, you can search for the smallest number that each denominator will divide into evenly. *Try multiplying the **larger denominator** by 2, 3, 4... and look at each answer to see if the smaller denominator*

will divide evenly into it. The first number that the smaller denominator will divide into can be used as a common denominator.

**Example:** Find a common denominator of  $\frac{3}{10}$  and  $\frac{4}{15}$ .

The denominators are 10 and 15.

$$15 \times 2 = 30$$

You can divide 10 into 30.

30 can be used as a common denominator.

**Example:** Find a common denominator of  $\frac{1}{6}$  and  $\frac{9}{10}$ .

$10 \times 2 = 20$       6 will not divide into 20. Try again.

$10 \times 3 = 30$       6 will divide into 30

So 30 can be used.

**Note:** This method gives the smallest possible common denominator but it can be time consuming.

**Method 3:** If the denominators have no common factor, multiply the two denominators together and use the answer as the common denominator. This method will always get a common denominator you can use, although it might not be the smallest one possible.

**Example:** Find the common denominator of  $\frac{2}{3}$  and  $\frac{4}{5}$ .

The denominators are 3 and 5.

$$\text{Multiply } 3 \times 5 = 15$$

15 is a common denominator.

One of these three methods will get you a common denominator. Once you have found a common denominator, continue with the next steps.

## Step 2: Change the original fractions to equivalent fractions with common denominators and add.

Using the common denominator we have found, we change the original fractions to **equivalent fractions** with that denominator. We will find equivalent fractions using the examples with their common denominators from this and the previous page. Then we will do the addition.

**Example 1:** We found the common denominator of  $\frac{3}{4}$  and  $\frac{5}{8}$  to be 8. Now we have to find an equivalent fraction for  $\frac{3}{4}$  with 8 as the denominator.

$$\begin{aligned} \frac{3}{4} &= \frac{?}{8} & 4 \times 2 &= 8 \text{ and } 3 \times 2 = 6 \\ &= \frac{6}{8} \end{aligned}$$

We don't have to do anything to change  $\frac{5}{8}$ .

Now we can add.

$$\begin{aligned} \frac{6}{8} + \frac{5}{8} \\ &= 1 \frac{1}{8} & \text{Change to a mixed number} \\ &= 1 \frac{3}{8} \end{aligned}$$

**Example 2:** The common denominator of  $\frac{2}{3}$  and  $\frac{4}{5}$  is 15. Now we find equivalent fractions with 15 as the denominator.

$$\begin{aligned}\frac{2}{3} &= \frac{?}{15} \\ &= \frac{10}{15}\end{aligned}$$

$$\begin{aligned}\frac{4}{5} &= \frac{?}{15} \\ &= \frac{12}{15}\end{aligned}$$

Now we add:

$$\begin{aligned}\frac{10}{15} + \frac{12}{15} \\ &= \frac{22}{15} && \text{Change to a mixed number} \\ &= 1 \frac{7}{15}\end{aligned}$$

**Example 3:** The common denominator of  $\frac{3}{10}$  and  $\frac{4}{15}$  is 30. Next we find equivalent fractions.

$$\begin{aligned}\frac{3}{10} &= \frac{?}{30} \\ &= \frac{9}{30}\end{aligned}$$

$$\begin{aligned}\frac{4}{15} &= \frac{?}{30} \\ &= \frac{8}{30}\end{aligned}$$

Now we add:

$$\frac{9}{30} + \frac{8}{30} = \frac{17}{30} \quad \frac{17}{30} \text{ is in lowest terms}$$

### ***Adding More than Two Fractions Together***

Before three or more fractions can be added, they all have to have common denominators. If they don't already have common denominators, change them to equivalent fractions with common denominators.

**Example:** Add  $\frac{3}{4} + \frac{3}{8} + \frac{11}{16}$ .

See if you can use the largest denominator as the common denominator. 4 and 8 will divide evenly into 16, so 16 can be used as the common denominator.

$$\frac{3}{4} = \frac{?}{16}$$

$$\frac{3}{4} = \frac{12}{16}$$

$$\frac{3}{8} = \frac{?}{16}$$

$$\frac{3}{8} = \frac{6}{16}$$

$\frac{11}{16}$  already has 16 as its denominator.

Now add:

$$\begin{aligned}\frac{12}{16} + \frac{6}{16} + \frac{11}{16} & && 12 + 6 + 11 = 29 \\ &= \frac{29}{16}\end{aligned}$$

Change  $\frac{29}{16}$  to a mixed number.

$$\frac{29}{16} = 1 \frac{13}{16}$$

**Example:** Add  $\frac{1}{4} + \frac{2}{5} + \frac{3}{8}$ .

If you can't use the largest denominator as a common denominator, find a number that all the denominators will divide into evenly. Multiply the largest denominator by 2, 3, 4 and so on, each time seeing if the other denominators will divide evenly into the multiplication answer. When you get a number that each denominator will divide into evenly, use that as your common denominator. We have written down all steps but you can do the multiplying and dividing in your head.

8 is the largest denominator.  
 $8 \times 2 = 16$       4 will go into 16 but 5 won't  
 $8 \times 3 = 24$       this won't work either  
 $8 \times 4 = 32$       won't work  
 $8 \times 5 = 40$       denominators 4, 5 and 8 will all divide into 40

Now find equivalent fractions with 40 as the denominator.

$$\frac{1}{4} = \frac{?}{40}$$
$$\frac{1}{4} = \frac{10}{40}$$

$$\frac{2}{5} = \frac{?}{40}$$
$$\frac{2}{5} = \frac{16}{40}$$

$$\frac{3}{8} = \frac{?}{40}$$
$$\frac{3}{8} = \frac{15}{40}$$

Add the equivalent fractions.

$$\frac{10}{40} + \frac{16}{40} + \frac{15}{40}$$
$$= \frac{41}{40}$$
$$= 1 \frac{1}{40}$$

$10 + 16 + 15 = 41$   
Change to a mixed number

**Example:** Add  $2 \frac{3}{8} + 4 \frac{1}{6}$ .

Add the whole numbers.

$$2 + 4 = 6$$

Add the fractions  $\frac{3}{8}$  and  $\frac{1}{6}$ .

$$\frac{3}{8} + \frac{1}{6}$$
$$= \frac{9}{24} + \frac{4}{24}$$
$$= \frac{13}{24}$$

24 is a common denominator  
 $9 + 4 = 13$

Combine the whole number and the fraction.

$$6 + \frac{13}{24} = 6 \frac{13}{24}$$

do this step in your head

Thus:

$$2 \frac{3}{8} + 4 \frac{1}{6} = 6 \frac{13}{24}$$

You can add the whole numbers in the same step that you add the fractions, as long as you keep the two operations separate.

**Example:** Add  $5 \frac{2}{3} + 4 \frac{1}{4}$ .

$$\begin{aligned} & 5 \frac{2}{3} + 4 \frac{1}{4} \\ &= 5 \frac{8}{12} + 4 \frac{3}{12} \\ &= 9 \frac{11}{12} \end{aligned}$$

If the fraction part of the answer is an improper fraction, it must be changed to a mixed number. Then add the two whole numbers. Combine this answer with the new fraction.

**Example:** Add  $4 \frac{2}{7} + 9 \frac{6}{7}$ .

$$\begin{aligned} & 4 \frac{2}{7} + 9 \frac{6}{7} \\ &= 13 \frac{8}{7} \end{aligned}$$

$$\begin{aligned} & \frac{8}{7} && \text{change improper fraction to a mixed number.} \\ & \frac{8}{7} = 1 \frac{1}{7} \end{aligned}$$

$$\begin{aligned} & 13 + 1 \frac{1}{7} && \text{Add the two whole numbers } 13 + 1 = 14 \\ &= 14 \frac{1}{7} \end{aligned}$$

**Example:** Add  $5 \frac{4}{5} + 2 \frac{2}{3}$ .

$$\begin{aligned} & 5 \frac{4}{5} + 2 \frac{2}{3} \\ &= 5 \frac{12}{15} + 2 \frac{10}{15} \\ &= 7 \frac{22}{15} \\ &= 7 + 1 \frac{7}{15} \\ &= 8 \frac{7}{15} \end{aligned}$$

$$\frac{22}{15} = 1 \frac{7}{15}$$

### TO ADD FRACTIONS OR MIXED NUMBERS WITH DIFFERENT DENOMINATORS

1. First find a common denominator using one of the methods below:
  - See if the smaller denominator will divide evenly into the larger ones.
  - Search for a common denominator by multiplying the largest denominator by 2, 3, 4 ... and see if the others will divide evenly into the answer. If they do, that answer can be used as the common denominator.
  - Multiply the denominators together.
  - You can also find a common denominator by identifying in your head any number that all denominators will divide into evenly.
2. After finding a common denominator, change the fractions to equivalent fractions with that denominator.
3. Add the numerators of the equivalent fractions and place the sum over the common denominator.
4. If necessary, change any improper fractions to mixed numbers, add the whole numbers together and reduce the fraction to lowest terms.

7. Do these questions involving addition of fractions. **Answers are at the end of this skills manual.**

a)  $\frac{1}{8} + \frac{3}{4}$

b)  $9\frac{1}{3} + \frac{2}{5}$

c)  $\frac{4}{5} + \frac{2}{7}$

d)  $4\frac{1}{3} + \frac{5}{12}$

e)  $8\frac{1}{2} + \frac{2}{3}$

f)  $2\frac{3}{8} + 4\frac{5}{6}$

g)  $\frac{4}{9} + \frac{5}{27}$

h)  $\frac{3}{10} + \frac{5}{6}$

i)  $\frac{7}{11} + \frac{1}{3}$

j)  $\frac{3}{4} + \frac{3}{8} + \frac{1}{2}$

k)  $\frac{3}{4} + \frac{1}{8} + \frac{4}{5}$

l)  $2\frac{5}{6} + 4\frac{2}{3} + 6\frac{5}{8}$

8. In one week, a caterer worked  $7\frac{1}{2}$  hours,  $5\frac{1}{4}$  hours, 9 hours,  $7\frac{3}{4}$  hours and  $8\frac{1}{2}$ . What was the total number of hours she worked?
9. A baker was planning to make several different cake recipes. One called for  $5\frac{3}{4}$  cups of flour, one called for  $4\frac{1}{2}$  cups, one called for  $3\frac{1}{3}$  cups and one called for  $6\frac{2}{3}$  cups. How many cups of flour did the baker need in total to make the cakes?

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## ***SUBTRACTING FRACTIONS***

The rules for subtracting fractions are similar to those for adding.

### **To subtract fractions with the same denominator:**

1. Write the two fractions so the one you are subtracting from is written first.
2. Subtract one numerator from the other.
3. Put the answer over the original denominator.
4. Reduce the answer to lowest terms if necessary.

**Example:** Subtract  $5/8 - 1/8$ .

$$5/8 - 1/8$$

$$5 - 1 = 4$$

Subtract the numerators.

$$5/8 - 1/8 = 4/8$$

Put the subtraction answer 4 as the new numerator over the original denominator 8.

$$4/8 = 1/2$$

Reduce to lowest terms. 2 is the common factor.

### **To subtract fractions if the denominators are *not* the same:**

1. Change the fractions to equivalent fractions with a common denominator.
2. Subtract as above.

**Example:**  $1/2 - 1/6$

$$1/2 = 3/6$$

The common denominator is 6. Change  $1/2$  to an equivalent fraction with the denominator 6.

$$3/6 - 1/6$$

Now subtract. ( $3 - 1 = 2$ )

$$= 2/6$$

Reduce to lowest terms

$$= 1/3$$

### **To subtract mixed numbers:**

1. Subtract the whole numbers.
2. Subtract the fractions.
3. Borrow if necessary.

**Example:**  $7 \frac{5}{8} - 4 \frac{3}{8}$

$$7 - 4 = 3$$

Subtract the whole numbers.

$$5/8 - 3/8$$

Subtract the fractions

$$= 2/8$$

Reduce to lowest terms

$$= 1/4$$

$$7 \frac{5}{8} - 4 \frac{3}{8}$$

Put the whole number answer with the fraction answer.

$$= 3 \frac{1}{4}$$

You could do both steps in the same line.

$$\begin{aligned}7 \frac{5}{8} - 4 \frac{3}{8} \\= 3 \frac{2}{8} \\= 3 \frac{1}{4}\end{aligned}$$

**Example:**  $4 \frac{5}{8} - 2 \frac{1}{4}$

$$\frac{1}{4} = \frac{2}{8} \quad \text{The common denominator is 8.}$$

$$\begin{aligned}4 \frac{5}{8} - 2 \frac{2}{8} \\= 2 \frac{3}{8}\end{aligned}$$

**Example:**  $10 \frac{4}{9} - 1 \frac{1}{6}$

$$\frac{4}{9} = \frac{8}{18} \quad \text{The common denominator is 18.}$$

$$\frac{1}{6} = \frac{3}{18}$$

$$\begin{aligned}10 \frac{8}{18} - 1 \frac{3}{18} \\= 9 \frac{5}{18}\end{aligned}$$

### ***Borrowing in Subtraction of Fractions***

When you subtract mixed numbers, the numerator of the first fraction may be smaller than the numerator of the second one. An example is  $8 \frac{1}{3} - 6 \frac{2}{3}$ . You can't subtract the fractions as they are because  $\frac{1}{3}$  is smaller than  $\frac{2}{3}$ .

#### **To borrow for subtraction of fractions:**

1. ***Borrow*** 1 from the first whole number.
  - This reduces the whole number to one less than before.
  - If the first whole number was 8, it now becomes 7.
2. ***Convert*** the borrowed 1 to a fraction with the same denominator as the first fraction.
  - Remember, the number 1 can be written as a fraction with any denominator, as long as it has the same numerator and denominator.
  - For example,  $1 = \frac{3}{3}$ .
3. ***Add*** the 1, now in fraction form, to the first fraction.
  - The first fraction now has a larger numerator than the second fraction.
4. ***Subtract***.

---

**Example:** Subtract  $8 \frac{1}{3} - 6 \frac{2}{3}$ .

**Step 1:** Borrow or take away 1 from the 8.

$$8 - 1 = 7$$

**Step 2:** Change the borrowed 1 to a fraction.

Since any number written over itself is one,  $1 = \frac{3}{3}$

**Step 3:** Add the borrowed 1 to the fraction.

$$8 \frac{1}{3} = 7 + \frac{3}{3} + \frac{1}{3}$$

$$8 \frac{1}{3} = 7 \frac{4}{3}$$

**Step 4:** Now subtract, following the rules for subtraction of fractions:

$$8 \frac{1}{3} - 6 \frac{2}{3}$$

$$= 7 \frac{4}{3} - 6 \frac{2}{3}$$

$$= 1 \frac{2}{3}$$

### **Borrowing from a whole number**

You will also have to borrow when you subtract a fraction from a whole number.

**Example:** Subtract  $6 - \frac{1}{4}$ .

$$6 - 1 = 5 \quad \text{Borrow 1 from the 6.}$$

Change the borrowed 1 to a fraction with the same denominator as  $\frac{1}{4}$ . Since the denominator is 4, the 1 becomes the  $\frac{4}{4}$ . The 6 becomes a mixed number. Substitute  $5 \frac{4}{4}$  for the 6. Subtract.

$$6 - \frac{1}{4}$$

$$= 5 \frac{4}{4} - \frac{1}{4} \quad 4 - 1 = 3$$

$$= 5 \frac{3}{4}$$

Here is how to subtract a mixed number from a whole number:

**Example:** Subtract  $9 - 4 \frac{2}{3}$ .

$$9 - 1 = 8 \quad \text{Borrow 1 from 9.}$$

$$1 = \frac{3}{3} \quad \text{Change the borrowed 1 to a fraction with a denominator of 3.}$$

$$9 - 4 \frac{2}{3}$$

$$= 8 \frac{3}{3} - 4 \frac{2}{3} \quad \text{The 9 becomes the mixed number } 8 \frac{3}{3}.$$

$$= 4 \frac{1}{3}$$

**Note:** *If fractions do not have common denominators, you can only tell if you have to borrow after they are given common denominators.*

**Example:**  $5 \frac{1}{4} - 3 \frac{2}{5}$

$5 \frac{5}{20} - 3 \frac{8}{20}$  Common denominator is 20.  
The numerator 5 is smaller than the numerator 8.  
Borrow 1 from the whole number 5. (5 becomes 4.)  
Change the borrowed 1 to a fraction with the new denominator, 20.  
The fraction is  $\frac{20}{20}$ .  
Add it to existing fraction  $\frac{5}{20}$  to get  $\frac{25}{20}$ .

$$5 \frac{5}{20} = 4 \frac{25}{20}$$

Now subtract.

$$\begin{array}{r} 5 \frac{5}{20} - 3 \frac{8}{20} = \\ 4 \frac{25}{20} - 3 \frac{8}{20} \qquad 25 - 8 = 17 \\ = 1 \frac{17}{20} \end{array}$$

### TO SUBTRACT FRACTIONS

1. If the fractions have the same denominators, subtract one numerator from the other, and place the answer over the same denominator.
2. If the fractions have different denominators, change to equivalent fractions with a common denominator, and subtract as above.
3. Reduce to lowest terms.

### TO SUBTRACT MIXED NUMBERS

1. Subtract the whole numbers separately from the fractions.
2. If the second fraction is larger than the first, you can borrow from the first whole number to make the first fraction larger than the second. Then subtract as above.
3. If the first number is a whole number, borrow 1 from it and change that into a fraction equal to 1 with the same denominator as the fractional part of the other number. Then subtract.
4. Reduce to lowest terms.

10. Do these questions involving subtraction of fractions. **Answers are at the end of this skills manual.**

a)  $\frac{7}{9} - \frac{5}{9}$

b)  $\frac{3}{4} - \frac{1}{3}$

c)  $\frac{5}{8} - \frac{1}{4}$

d)  $\frac{2}{3} - \frac{5}{12}$

e)  $6 \frac{4}{5} - 2 \frac{3}{5}$

f)  $4 \frac{1}{2} - \frac{3}{8}$

g)  $7 \frac{9}{10} - 3 \frac{2}{5}$

h)  $15 \frac{3}{4} - 10 \frac{2}{3}$

i)  $9 \frac{11}{12} - \frac{3}{8}$

j)  $5 \frac{1}{3} - 2 \frac{2}{3}$

k)  $9 \frac{1}{4} - \frac{3}{4}$

l)  $5 \frac{1}{2} - 2 \frac{3}{4}$

m)  $7 - \frac{1}{5}$

n)  $8 - 2 \frac{1}{3}$

o)  $12 - 11 \frac{2}{3}$

- 
11. A container holds  $2\frac{3}{4}$  L of water. How much water is left if  $\frac{2}{3}$  L are poured out?
12. A side of beef weighing  $105\frac{1}{4}$  pounds was barbequed. After cooking for 6 hours, the beef weighed  $97\frac{1}{2}$  pounds. What was the loss in weight?
13. A portion of filo pastry measuring  $7\frac{3}{10}$  centimeters is cut from a piece 10 centimeters long. How much of the pastry is left?
14. A baker worked  $1\frac{1}{4}$  hours making rolls,  $3\frac{3}{4}$  hours making bread and  $1\frac{1}{2}$  hours making bagels. How much time does he have left to work if he works an eight hour day?

### ***MULTIPLICATION OF FRACTIONS***

#### **To multiply two fractions:**

1. Write the two fractions beside each other with a multiplication sign between them.
2. Reduce terms if possible and if desired.
3. Multiply the numerators together to get the new numerator.
4. Multiply the denominators together to get the new denominator.
5. Write your answer with the new numerator and denominator.
6. *Reduce the answer to lowest terms* and change any improper fractions to mixed numbers.

#### **Special cases:**

1. To multiply a mixed number and a fraction, or two mixed numbers,
  - Change all mixed numbers to improper fractions before multiplying.
2. To multiply a fraction by a whole number,
  - Place the whole number over 1 to make it an improper fraction.
    - This is not necessary but might make it easier for you in some cases.

**Example:**  $\frac{3}{4} \times \frac{1}{2}$

$$\begin{array}{l} \frac{3}{4} \times \frac{1}{2} \\ = \frac{3}{8} \end{array} \quad \begin{array}{l} \frac{3 \times 1 = 3}{4 \times 2 = 8} \quad \text{multiply numerators together,} \\ \text{then denominators} \end{array}$$

**Example:**  $\frac{2}{3} \times 7$

Place the whole number 7 over 1 to make an improper fraction. Then multiply the numerators and denominators together.

$$\begin{array}{l} \frac{2}{3} \times \frac{7}{1} \\ = \frac{14}{3} \\ = 4\frac{2}{3} \end{array} \quad \begin{array}{l} \frac{2 \times 7 = 14}{3 \times 1 = 3} \quad \text{multiply numerators together,} \\ \text{then denominators} \end{array}$$

change improper fraction to mixed number

**Example:**  $1\frac{4}{5} \times \frac{7}{8}$

$\frac{9}{5} \times \frac{7}{8}$  Change the mixed number  $1\frac{4}{5}$  to the improper fraction  $\frac{9}{5}$ . Then multiply.

$$\begin{array}{l} \frac{9}{5} \times \frac{7}{8} \\ = \frac{63}{40} \\ = 1\frac{23}{40} \end{array}$$

**Example:**  $2\frac{1}{3} \times 2\frac{2}{5}$

$$\begin{array}{l} = \frac{7}{3} \times \frac{12}{5} \\ = \frac{84}{15} \\ = 5\frac{9}{15} \\ = 5\frac{3}{5} \end{array}$$

You can **reduce terms** before you multiply. This will give you smaller numbers to work with. Divide any common factor into any two numbers on **opposite** sides of the fraction line. Look again at the third step in the last example.

3 and 12 are on opposite sides of the fraction line and have 3 as a common factor. Divide like this:

$$\begin{array}{l} \frac{7 \times \cancel{12}^4}{\cancel{3}_1 \times 5} \quad 12 \div 3 = 4 \\ \quad \quad \quad 3 \div 3 = 1 \end{array}$$

$$\begin{array}{l} = \frac{7 \times 4}{1 \times 5} \\ = \frac{28}{5} \end{array}$$

you don't need to write this step

$$= 5 \frac{3}{5}$$

change to a mixed number

You get the same answer but the numbers you multiplied were smaller. Reducing terms isn't essential but smaller numbers are easier to work with.

### TO MULTIPLY FRACTIONS

1. First change mixed numbers to improper fractions and place any whole numbers over 1.
2. Reduce any terms on opposite sides of the fraction line that have common factors.
3. Multiply the numerators together to get the new numerator.
4. Multiply the denominators together to get the new denominator.
5. Change any improper fraction in the answer to a mixed number.
6. Reduce the answer to lowest terms.

15. Do these questions involving multiplication of fractions. **Answers are at the end of this skills manual.**

a)  $4 \times \frac{3}{5}$

b)  $\frac{2}{7} \times 3$

c)  $\frac{1}{4} \times \frac{3}{8}$

d)  $\frac{11}{15} \times \frac{2}{3}$

e)  $2 \frac{3}{4} \times \frac{1}{2}$

f)  $3 \frac{1}{5} \times 7$

g)  $6 \times 2 \frac{4}{5}$

h)  $\frac{4}{9} \times 1 \frac{1}{3}$

i)  $\frac{7}{10} \times \frac{3}{4}$

16. A cook that is paid \$28 per hour gets time and a half for overtime. What is the hourly rate for overtime?

17. A recipe calls for 2 cups flour, 2 teaspoons baking powder, 1 tablespoon sugar,  $\frac{1}{4}$  cup butter and  $\frac{3}{4}$  cup milk. If the recipe needs to be tripled, how much of each ingredient will be required? (If a recipe is tripled, you need three times the amount of everything. Multiply each ingredient by 3.)

18. A food processor costs \$450. The purchaser puts  $\frac{1}{3}$  down and pays the rest in 6 equal monthly payments. What is the amount of the monthly payments?

---

## ***DIVIDING FRACTIONS***

Dividing fractions is fairly easy now that you can multiply them.

### ***To divide fractions:***

1. ***Invert the fraction you are dividing by and then multiply.***
  - When a fraction is **inverted**, it is turned upside down.

An inverted fraction is the **reciprocal fraction** of the original fraction.

Here are some reciprocal fractions:

$3/4$  inverted is  $4/3$

$4/1$  inverted is  $1/4$

$1/3$  inverted is  $3/1$

### **To divide a whole number, a mixed number or a fraction by a fraction:**

1. Change any mixed numbers to improper fractions.
2. If any number is a whole number, write the whole number over 1 to make it a fraction.
3. Invert the fraction that comes *after the sign*.
4. *Change the division sign to a multiplication sign.* You can reduce terms now.
5. Multiply the two fractions
6. Write the answer in lowest terms.

#### **Example:** $4 \div 1/4$

$4 \div 1/4$           invert the 2<sup>nd</sup> fraction  $1/4$  to  $4/1$ ,

$= 4/1 \times 4/1$         change the  $\div$  sign to a  $\times$  sign

$= 16/1$              write the whole number as a fraction over 1, then multiply

$= 16$

---

**Example:**  $8 \div 2 \frac{1}{3}$

$$\begin{aligned} 8 \div 2 \frac{1}{3} & \quad \text{change } 2 \frac{1}{3} \text{ to } \frac{7}{3} \\ = 8 \div \frac{7}{3} \\ = \frac{8}{1} \times \frac{3}{7} & \quad \text{invert } \frac{7}{3} \text{ to } \frac{3}{7}, \text{ change the } \div \text{ sign to a } \times \text{ sign} \\ = \frac{24}{7} & \quad \text{multiply} \\ = 3 \frac{3}{7} & \quad \text{change to a mixed number} \end{aligned}$$

**Example:**  $\frac{2}{5} \div \frac{2}{3}$

$$\begin{aligned} = \frac{2}{5} \times \frac{3}{2} & \quad \text{invert } \frac{2}{3} \text{ to } \frac{3}{2}, \text{ change the } \div \text{ sign to a } \times \text{ sign} \\ = \frac{6}{10} & \quad \text{multiply} \\ = \frac{3}{5} & \quad \text{reduce to lowest terms} \end{aligned}$$

**Example:**  $\frac{3}{4} \div 6$

$$\begin{aligned} = \frac{3}{4} \div \frac{6}{1} & \quad \text{write the whole number } 6 \text{ as a fraction over } 1 \\ = \frac{3}{4} \times \frac{1}{6} & \quad \text{invert } \frac{6}{1} \text{ to } \frac{1}{6}, \text{ change the } \div \text{ sign to a } \times \text{ sign} \\ = \frac{\overset{1}{\cancel{3}} \times 1}{4 \times \overset{2}{\cancel{6}}} & \quad \text{reduce terms, then multiply} \\ = \frac{1}{8} \end{aligned}$$

**Example:**  $1 \frac{1}{5} \div 2 \frac{1}{2}$

$$\begin{aligned} 1 \frac{1}{5} \div 2 \frac{1}{2} & \quad \text{change } 1 \frac{1}{5} \text{ to } \frac{6}{5} \text{ and } 2 \frac{1}{2} \text{ to } \frac{5}{2} \\ = \frac{6}{5} \div \frac{5}{2} \\ = \frac{6}{5} \times \frac{2}{5} \\ = \frac{12}{25} \end{aligned}$$

**Example:**  $4 \frac{3}{12} \div 8 \frac{5}{6}$

$$\begin{aligned} 4 \frac{3}{12} \div 8 \frac{5}{6} \\ = \frac{51}{12} \div \frac{53}{6} \\ = \frac{51}{12} \times \frac{6}{53} \\ = \frac{\overset{1}{\cancel{51}} \times \overset{1}{\cancel{6}}}{\underset{2}{12} \times 53} \\ = \frac{51}{106} \end{aligned}$$

### TO DIVIDE FRACTIONS

1. Change any mixed numbers to improper fractions. Change any whole numbers to fractions by writing them over 1.
2. Invert the second fraction.
3. Change the division sign to a multiplication sign.
4. Reduce any terms with common factors on opposite sides of the fraction line after inverting.
5. Multiply the numerators together and multiply the denominators together.
6. Write the new numerator over the new denominator, reducing the answer to lowest terms.

19. Do these questions to practice division with fractions. **Answers are on the last page.**

- |                            |                                       |                           |
|----------------------------|---------------------------------------|---------------------------|
| a) $5 \div 1/2$            | b) $1/3 \div 3/4$                     | c) $9/10 \div 3$          |
| d) $2/5 \div 8/25$         | e) $5 \frac{2}{5} \div 3/10$          | f) $4 \frac{2}{3} \div 7$ |
| g) $15 \div 1 \frac{1}{9}$ | h) $2 \frac{1}{6} \div 3 \frac{1}{4}$ | i) $4/5 \div 4/5$         |

20. A recipe for salad dressing calls for 2 cups oil,  $3/4$  cup lemon juice,  $1/3$  cup soy sauce, 2 teaspoons honey and 1 tablespoon fresh dill. If only half the amount of the recipe is to be prepared, how much of each ingredient is required? (Divide each amount by 2.)

21. A cook has  $3/5$  of a large pot of stock left. If the leftover stock needs to be divided into 3 equal portions, what fraction of the original amount of stock will each portion be?  
If the stockpot originally held 5 liters of stock, what is the amount of each of divided portions?

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## FRACTIONS WITH A CALCULATOR

Most calculators do not work directly with fractions. To do operations with fractions use the calculator to change fractions into decimals before you can add, subtract, multiply, or divide.

### Changing a fraction to a decimal with a calculator

You can change any fraction to a decimal by dividing the numerator by its denominator. To do this key in the numerator followed by the division sign and then key in the denominator.

**Example:** Change the fraction  $1/4$  to a decimal.

Divide the numerator 1 by the denominator 4.

Key in 1, the division sign, then 4.

The answer will be .25

**Addition:** Change all fractions to decimals by dividing the numerator by the denominator. The answer will be a decimal number. Add the decimal numbers.

**Example:** You have to keep track of your hours. In one day, you worked  $3\frac{1}{2}$  hours at one job, then  $1\frac{3}{4}$  hours at a second and  $2\frac{1}{4}$  hours at the third job. How many hours did you work that day?

Change the mixed numbers to decimals. To do this leave the whole number as it is and divide the numerator of the fraction by the denominator. This changes the fraction part to a decimal. Attach the decimal to its whole number.

$$3\frac{1}{2} = 3.5 \qquad 1 \div 2 = .5$$

$$1\frac{3}{4} = 1.75 \qquad 3 \div 4 = .75$$

$$2\frac{1}{4} = 1.25 \qquad 1 \div 4 = .25$$

Use your calculator to add.  $3.5 + 1.75 + 1.25 = 6.5$ .

You worked 6.5 or  $6\frac{1}{2}$  hours that day.

**Subtraction:** Change any fraction to a decimal number by dividing the numerator by the denominator. Then subtract the decimal numbers with the calculator.

**Multiplication:** Change all fractions to decimals, then multiply.

**Division:** Change all fractions to decimals, then divide.

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**ANSWER PAGE**

**CHANGING MIXED NUMBERS TO IMPROPER FRACTIONS**

1. a)  $23/7$       b)  $11/6$       c)  $21/4$       d)  $23/8$       e)  $32/3$       f)  $31/5$

**REDUCING FRACTIONS TO LOWEST TERMS**

2. a)  $2/3$       b)  $1/3$       c)  $1/4$       d)  $2$       e)  $1/8$       f)  $2/5$

**CHANGING IMPROPER FRACTIONS TO MIXED NUMBERS**

3. a)  $1\ 1/3$       b)  $3$       c)  $3\ 2/7$       d)  $9\ 9/10$       e)  $6$       f)  $2\ 1/2$   
4. a)  $24/40$       b)  $3/9$       c)  $60/18$       d)  $15/24$       e)  $3/12$       f)  $6/21$

**ADDING FRACTIONS OR MIXED NUMBERS WITH THE SAME DENOMINATOR**

5. a)  $6/7$       b)  $4/4 = 1$       c)  $1\ 1/2$       d)  $6\ 3/5$       e)  $14\ 1/3$       f)  $13$   
g)  $1\ 1/8$       h)  $7\ 11/12$       i)  $8\ 1/10$   
6.  $4\ 2/3$  liters

**ADDING FRACTIONS OR MIXED NUMBERS WITH DIFFERENT DENOMINATORS**

7. a)  $7/8$       b)  $9\ 11/15$       c)  $1\ 3/35$       d)  $4\ 3/4$       e)  $9\ 1/6$       f)  $7\ 5/24$   
g)  $17/27$       h)  $1\ 2/15$       i)  $32/33$       j)  $1\ 5/8$       k)  $1\ 27/40$       l)  $14\ 1/8$   
8. 38 hours  
9.  $20\ 1/4$  cups

**SUBTRACTING FRACTIONS**

10. a)  $2/9$       b)  $5/12$       c)  $3/8$       d)  $1/4$       e)  $4\ 1/5$       f)  $4\ 1/8$   
g)  $4\ 1/2$       h)  $5\ 1/12$       i)  $9\ 13/24$       j)  $2\ 2/3$       k)  $8\ 1/2$       l)  $2\ 3/4$   
m)  $6\ 4/5$       n)  $5\ 2/3$       o)  $1/3$   
11.  $2\ 1/12$  liters  
12.  $7\ 3/4$  pounds

13.  $2\frac{7}{10}$  centimeters

14. He works a total of  $6\frac{1}{2}$  hours, so he has  $1\frac{1}{2}$  hours left out of an 8 hour day.

### MULTIPLYING FRACTIONS

15. a)  $2\frac{2}{5}$     b)  $\frac{6}{7}$     c)  $\frac{3}{32}$     d)  $\frac{22}{45}$     e)  $1\frac{3}{8}$     f)  $22\frac{2}{5}$

g)  $16\frac{4}{5}$     h)  $\frac{16}{27}$     i)  $\frac{21}{40}$

16. \$42. per hour

17. 6 cups flour  
6 teaspoons baking powder  
3 tablespoons sugar  
 $\frac{3}{4}$  cups butter  
 $2\frac{1}{4}$  cups milk

18.  $\frac{1}{3} \times \$450. = \$150.$   
 $\$450. - \$150. = \$300$   
 $\$300 \div 6 = \$50$  per month payment

### DIVIDING FRACTIONS

19 a) 10    b)  $\frac{4}{9}$     c)  $\frac{3}{10}$     d)  $1\frac{1}{4}$     e) 18    f)  $\frac{2}{3}$

g)  $13\frac{1}{2}$     h)  $\frac{2}{3}$     i) 1

20. 1 cup oil  
 $\frac{3}{8}$  cup lemon juice  
 $\frac{1}{6}$  cup soy sauce  
1 teaspoon honey  
 $\frac{1}{2}$  tablespoon dill

21.  $\frac{1}{5}$  of the original amount  
1 liter